

Total No. of Questions : 9]

SEAT No. :

PA-1182

[Total No. of Pages : 7

[5925]-204

S.E. (Civil)

**ENGINEERING MATHEMATICS - III
(2019 Pattern) (Semester - III) (207001)**

Time : 2½ Hours]

[Max. Marks : 70

Instructions to the candidates:

- 1) *Question No. 1 is compulsory.*
- 2) *Attempt Q.2 or Q.3, Q.4 or Q.5, Q.6 or Q.7, Q.8 or Q.9.*
- 3) *Assume suitable data, if necessary.*
- 4) *Neat diagrams must be drawn wherever necessary.*
- 5) *Figures to the right indicates full marks.*
- 6) *Use of electronic pocket calculator is allowed.*

Q1) a) The pair of regression Lines are $L1 : 8x - 10y + 66 = 0$ and

$$L2 : 40x - 18y = 214 \quad [1]$$

- i) L1 is the regression Line y on x .
- ii) L1 is the regression line x on y .
- iii) L2 is regression line y or x .
- iv) L1 and L2 is regression line x on y .

b) Vector along the direction of the line. [1]

$$\frac{x-1}{2} = \frac{y+2}{1} = \frac{z-3}{5} \text{ is}$$

- | | |
|--|---|
| i) $\frac{\hat{i} - 2\hat{j} - 3\hat{k}}{\sqrt{14}}$ | ii) $\frac{\hat{i} + 2\hat{j} + 5\hat{k}}{\sqrt{30}}$ |
| iii) $\frac{2\hat{i} + \hat{j} - 5\hat{k}}{\sqrt{30}}$ | iv) $\frac{2\hat{i} + \hat{j} + 5\hat{k}}{\sqrt{30}}$ |

P.T.O.

Q2) a) A computer while calculating correlation coefficient between two variables X and Y from 25 pairs of observations obtained the following results :

$$n = 25, \sum X = 25, \sum X^2 = 650, \sum Y = 100, \sum Y^2 = 460, \sum XY = 508.$$

Later it was discovered that the values (X, Y) = (8, 12) was copied as (6, 14) and the value (8, 6) was copied as (6, 8). Obtain the correct value of the correlation coefficient. [5]

b) In a normal distribution 31% of the items are under 45 and 8% are above 64. Find the mean and standard deviation of the distribution. Take Area $(0 < z < 1.4) = 0.42$ and Area $(0 < z < 0.5) = 0.19$ where z is the standard normal variate. [5]

c) Verify at 5% level of significance and 4 degrees of freedom if the distribution can be assumed to be poisson given:

# defects :	0	1	2	3	4	5
Frequency :	6	13	13	8	4	3

Take $e^{-2} = 0.135$. in the calculations round off the frequencies to the immediate higher integral value. Take $\chi^2_{0.05} = 11.07$ [5]

OR

Q5) a) Find the directional derivative of $\phi = xy + yz^2$ at the point $(1, -1, 1)$ to wards point $(2, 1, 2)$. [5]

b) Prove the following identities (any one) [5]

i) $\nabla \times (\vec{a} \times \vec{r}) = 2\vec{a}$

ii) $\nabla(\vec{a} \cdot \vec{r}) = \vec{a}$

c) Show that $\vec{F} = (xy^2 + xz^2)\hat{i} + (yx^2 + yz^2)\hat{j} + (zx^2 + zy^2)\hat{k}$ is irrotational. Find scalar ϕ such that $\vec{F} = \nabla \phi$ [5]

Q6) a) Evaluate $\int_C \vec{F} \cdot d\vec{r}$ along the straight line joining points $(0, 0, 0)$ and $(2, 1, 3)$ where $\vec{F} = 3x^2\hat{i} + (2xz - y)\hat{j} + z\hat{k}$ [5]

b) Evaluate $\iiint_S (x\hat{i} + y\hat{j} + z\hat{k}) \cdot d\vec{s}$ over the surface of sphere $x^2 + y^2 + z^2 = 1$ [5]

c) Evaluate using Stoke's theorem $\iint_S (\nabla \times \vec{F}) \cdot d\vec{s}$ where $\vec{F} = y^2\hat{i} + z\hat{j} + xy\hat{k}$ and S is surface of paraboloid $z = 4 - x^2 - y^2 (z \geq 0)$. [5]

OR

Q7) a) Use Green's theorem to evaluate $\int_c (2x^2 - y^2) dx + (x^2 + y^2) dy$ where 'C' is boundary of area enclosed by the axis and circle $x^2 + y^2 = 16, z = 0$. [5]

b) Apply Stoke's theorem to evaluate $\int_c \vec{F} \cdot d\vec{r}$ where $\vec{F} = yz\vec{i} + zx\vec{j} + xy\vec{k}$ and S is upper part of sphere $x^2 + y^2 + z^2 = 1$ above XOY plane. [5]

c) Evaluate $\iint_s (x\vec{i} + y\vec{j} + z^2\vec{k}) \cdot d\vec{s}$. Where S is the surface of cylinder $x^2 + y^2 = 4$ bounded by planes $z = 0$ and $z = 2$. [5]

Q8) a) A string stretched and fastened between two points L a part. Motion is started by displacing the string in the form $y = a \sin \frac{\pi x}{L}$ from which it is released at time $t = 0$. Find the displacement $y(x, t)$. [8]

b) Solve the one dimensional heat equation $\frac{\partial y}{\partial t} = k \frac{\partial^2 u}{\partial x^2}$ subject to conditions.

i) u is finite $\forall t$.

ii) $u(0, t) = 0$,

iii) $u(\pi, t) = 0$,

iv) $u(x, 0) = \pi x - x^2 \quad 0 \leq x \leq \pi$ [7]

OR

Q9) a) A tightly stretched string with fixed ends $x = 0$ and $x = l$ is initially at rest in its equilibrium position is set to vibration by giving each point a velocity $3x(l - x)$ for $0 < x < l$. Find the displacement $y(x, t)$ at any time t . [8]

b) An infinitely long uniform metal plate is enclosed between lines $y = 0$, and $y = l$ for $x > 0$. The temperature is zero along the edges $y = 0$, $y = l$, and at infinity. If edge $x = 0$ is kept at a constant temperature v_0 , Find the temperature distribution $v(x, y)$. [7]

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